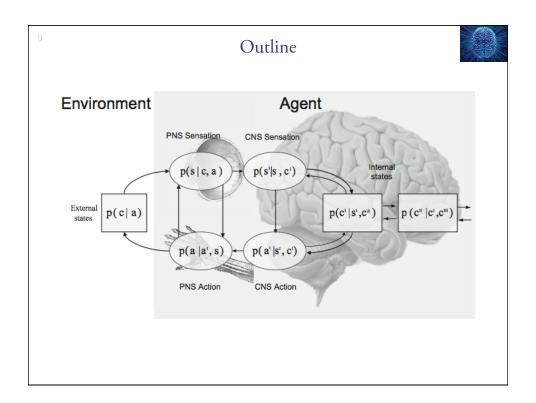


## The anticipating brain



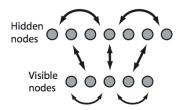
- 1) The brain can develop a model of the world, which can be used to anticipate or predict the environment.
- 2) The inverse of the model can be used to recognize causes by evoking internal concepts.
- Hierarchical representations are essential to capture the richness of the world.
- 4) Internal concepts are learned through matching the brain's hypotheses with input from the world.
- 5) An agent can learn actively by testing hypothesis through actions.
- 6) The temporal domain is an important degree of freedom.



## Recurrent networks with hidden nodes



### The Boltzmann machine:



Energy:  $H^{nm} = \frac{1}{2} \sum_{ij} w_{ij} s_i^n s_j^m$ 

Probabilistic update:  $p(s_i^n = +1) = \frac{1}{1 + \exp(-b \sum_j w_{ij} s_j^n)}$ 

Boltzmann-Gibbs distribution:  $p(\mathbf{s}^{v}; \mathbf{w}) = \frac{1}{Z} \sum_{m \in h} \exp(-\beta H^{vm})$ 

1

## Training Boltzmann machines



#### Kulbach-Leibler divergence

$$KL(p(\mathbf{s}^{v}), p(\mathbf{s}^{v}; \mathbf{w})) = \sum_{\mathbf{s}}^{v} p(\mathbf{s}^{v}) \log \frac{p(\mathbf{s}^{v})}{p(\mathbf{s}^{v}; \mathbf{w})}$$
$$= \sum_{\mathbf{s}}^{v} p(\mathbf{s}^{v}) \log p(\mathbf{s}^{v}) - \sum_{\mathbf{s}}^{v} p(\mathbf{s}^{v}) \log p(\mathbf{s}^{v}; \mathbf{w})$$

Minimizing KL is equivalent to maximizing the average log-likelihood function

$$I(\mathbf{w}) = \sum_{\mathbf{s}}^{v} p(\mathbf{s}^{v}) \log p(\mathbf{s}^{v}; \mathbf{w}) = \langle \log p(\mathbf{s}^{v}; \mathbf{w}) \rangle.$$

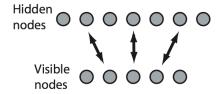
#### **Gradient decent** $\rightarrow$ **Boltzmann Learning**

$$\Delta w_{ij} = \eta \frac{\partial I}{\partial w_{ij}} = \eta \frac{\beta}{2} \left( \langle s_i s_j \rangle_{\text{clamped}} - \langle s_i s_j \rangle_{\text{free}} \right).$$

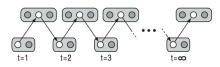
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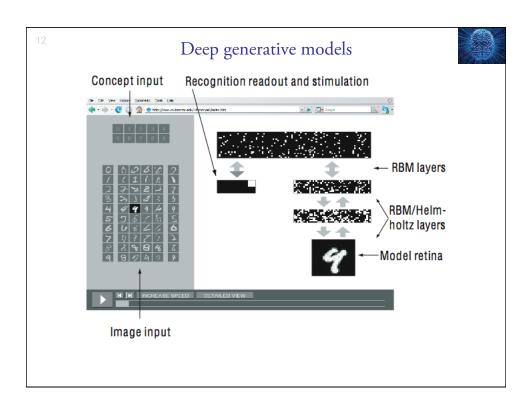
# The restricted Boltzmann machine

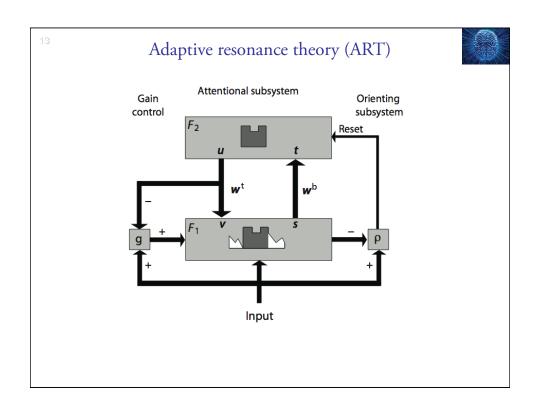




#### Contrastive Hebbian learning: Alternating Gibbs sampling







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## Further readings



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